(i) Printed Pages:	3	
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Roll No.

(ii) Questions :8

Sub. Code: 0 0 4 5

Exam. Code: 0 0 0 1

B.A./B.Sc. (General) 1st Semester

(1129)

MATHEMATICS

Paper-III

(Trigonometry and Matrices)

Time Allowed: Three Hours]

[Maximum Marks: 30

- Note:— (1) Attempt *five* questions in all by selecting at least *two* questions from each unit.
 - (2) All questions carry equal marks.

UNIT-I

- 1. (a) If $a = \cos\left(\frac{2\pi}{7}\right) + i \sin\left(\frac{2\pi}{7}\right)$, $b = a + a^2 + a^4$ and $c = a^3 + a^5 + a^6$, then show that b and c are roots of equation $x^2 + x + 2 = 0$.
 - (b) Find all value of $\left(\frac{1}{2} + i\frac{\sqrt{3}}{2}\right)^{3/4}$ and show that continued product of all the value is 1.
- 2. (a) State and prove De-Moivre's theorem for integral index.
 - (b) Show that each primitive 12^{th} root of unity statisfies $x^4 x^2 + 1 = 0$.

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[Turn over

3. (a) If $i^{i - \infty} = A + iB$ and only principal value are considered, prove that:

(i)
$$\tan \left(\frac{\pi A}{2}\right) = \frac{B}{A}$$

(ii)
$$A^2 + B^2 = e^{-\pi B}$$
.

- (b) Prove that $\log \left(\frac{\sin (x+iy)}{\sin (x-iy)} \right) = 2i \tan^{-1}(\cot x \tanh y)$.
- 4. (a) Sum to n terms the series $\sin \theta + \frac{1}{3} \sin 2\theta + \frac{1}{3^2} \sin 3\theta + \dots$
 - (b) Prove that $\lim_{x\to 0} \frac{1}{x^2} \log \left(\frac{\tan^{-1} x}{x} \right) = \frac{-1}{3}$.

UNIT—II

5. (a) Prove that every square matrix over C can be expressed uniquely as P + iQ, where P and Q are Hermitian matrices.

(b) Let
$$A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & -1 & -1 \\ 3 & 1 & 1 \end{bmatrix}$$
. Find non-singular matrices

P and Q such that PAQ is in normal form and hence determine rank of A.

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6. (a) Solve completely the system of equation:

$$x + 2y + 2z - s + 3t = 0$$

$$x + 2y + 3z + s + t = 0$$

$$3x + 6y + 8z + s + 5t = 0$$

(b) Show that rank of $\begin{bmatrix} a & b & c \\ b & c & a \\ c & a & b \end{bmatrix}$ is less than 3 iff either

$$a + b + c = 0$$
 or $a = b = c$.

7. (a) Investigate for what value of γ , μ the simultaneous equations:

$$x + y + z = 6$$

$$x + 2y + 3z = 10$$

$$x + 2y + \gamma z = \mu$$
 have

- (i) Unique solution
- (ii) No solution
- (iii) Infinite number of solutions.
- (b) Prove that characteristic roots of Hermitian matrix are real.
- 8. (a) If $A = \begin{bmatrix} 1 & 2 \\ -1 & 3 \end{bmatrix}$ then using Caley-Hamilton theorem express $A^6 4A^5 + 8A^4 12A^3 + 14A^2$ as linear polynomial in A.
 - (b) Diagonalize the following matrices, if possible:

$$A = \begin{bmatrix} 2 & 1 \\ 4 & 2 \end{bmatrix}$$

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